

Math 151 Week-In-Review 7

K.1, K.2, 3.7, 3.8 Todd Schrader

Problem Statements

1. Sketch a curve with the vector equation $\mathbf{r}(t) = \langle t - 1, 2t^2 \rangle$. Use a tangent vector to determine the direction of the curve as t increases.



2. If $r(t) = \langle t \cos(t), 4 \sin(t) \rangle$ represents the position of a particle at time t, find the velocity, acceleration, and speed of the particle when $t = \frac{\pi}{3}$.



3. Find a unit tangent vector to the curve $\mathbf{r}(t) = \langle 2te^{5t}, t^t \rangle$ when t = 2.



- 4. A curve has parametric equations $x = t^3 5t, y = t^2$.
 - (a) Find an expression for the slope of the tangent line to the curve, where it is defined.

(b) Find Cartesian equations of both tangent lines to the curve that pass through the point (0,5).

(c) Find the points where the tangent line to the curve is horizontal or vertical.



- 5. The graph of the parametric equations $x = r(\theta \sin \theta), y = r(1 \cos \theta)$ is called a cycloid.
 - (a) What are the coordinates of x and y when $\theta = 0$?

(b) Show that this cycloid has a vertical tangent at the origin.



- 6. The position of a particle is represented by $f(t) = \frac{9t}{t^2 + 9}$, $t \ge 0$, where t is measured in seconds and f(t) is measured in feet.
 - (a) Find the velocity at time t.

(b) What is the velocity after 1 second?

(c) When is the particle at rest?

(d) When is the particle moving in the positive direction?



(6	e) Find the total distance traveled in the first 6 seconds.
(1	f) Find the acceleration at time t .
3)	g) When is the particle accelerating in the positive direction?
(ł	n) When it the particle speeding up?
(i) When is the particle slowing down?



- 7. If a tank holds 5000 gallons of water, which drains from the bottom of the tank in 40 minutes, the Torricelli's Law gives the volume, V, of water remaining in the tank after t minutes according to the formula: $V = 5000 \left(1 \frac{1}{40}t\right)^2$, $0 \le t \le 40$.
 - (a) Find the rate at which water is draining from the tank after t minutes.

(b) Find the rate at which the water is draining after 5, 10, 20, and 40 minutes.

(c) At what time is water flowing out the fastest? The slowest?



- 8. A ball is thrown vertically upward with a velocity of 80ft/s. Its height after t seconds is $s = 80t 16t^2$.
 - (a) What is the maximum height reached by the ball?
 - (b) What is the velocity of the ball when it is 96ft above the ground on its way up? On its way down?
 - (c) With what velocity does the ball hit the ground?