

1. Evaluate the surface integral  $\iint_S (x + y + z) dS$ , where  $S$  is the parallelogram with parametric equations  $x = u + v$ ,  $y = 1 - v$ ,  $z = 1 + 2u + v$ ,  $0 \leq u \leq 2$ ,  $0 \leq v \leq 1$ .
2. Evaluate the surface integral  $\iint_S (x^2 z + y^2 z) dS$  where  $S$  is the part of the plane  $z = 4 + x + y$  that lies inside the cylinder  $x^2 + y^2 = 4$ .
3. Evaluate  $\iint_S (x^2 + y^2 + z^2) dS$ ,  $S$  is the part of the cylinder  $x^2 + y^2 = 9$  between the planes  $z = 0$  and  $z = 2$ , together with its top and bottom disks.
4. Find flux of the vector field  $\mathbf{F} = \langle x, y, 5 \rangle$  across the surface  $S$  which is the boundary of the region enclosed by the cylinder  $x^2 + z^2 = 1$  and the planes  $y = 0$  and  $x + y = 2$ . Use positive (outward) orientation for  $S$ .
5. Evaluate the surface integral  $\iint_S \langle x, y, 1 \rangle \cdot d\mathbf{S}$  where  $S$  is the portion of the paraboloid  $z = 1 - x^2 - y^2$  in the first octant, oriented by downward normals.
6. Evaluate  $\iint_S \mathbf{F} \cdot d\mathbf{S}$ , if  $\mathbf{F} = \langle y, z - y, x \rangle$ , and  $S$  is the surface of the tetrahedron with vertices  $(0,0,0)$ ,  $(1,0,0)$ ,  $(0,1,0)$ , and  $(0,0,1)$ .
7. Use Stokes' Theorem to evaluate  $\oint_C \mathbf{F} \cdot d\mathbf{r}$ , where  $\mathbf{F}(x, y, z) = \langle 3z, 5x, -2y \rangle$  and  $C$  is the ellipse in which the plane  $z = y + 3$  intersects the cylinder  $x^2 + y^2 = 4$ , with positive orientation as viewed from above.
8. Find the work performed by the force field  $\mathbf{F} = \langle -3y^2, 4z, 6x \rangle$  on a particle that traverses the triangle  $C$  in the plane  $z = \frac{1}{2}y$  with vertices  $A(2, 0, 0)$ ,  $B(0, 2, 1)$ , and  $O(0, 0, 0)$  with a counterclockwise orientation looking down the positive  $z$ -axis.